

# Boolean Function Reconstruction

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            4 seconds  
Memory limit:         1024 megabytes

Given the truth table of a boolean function with  $n$  boolean variables as input, construct an expression that satisfies this function. In the expression, you are only allowed to use the logical **and** (&) and logical **or** (|) operators.

Specifically, a truth table of a boolean function with  $n$  boolean variables gives all the  $2^n$  outputs corresponding to the possible values of  $n$  input variables. A boolean expression `<expr>` has the following forms:

- **T,F**: Represents **True** and **False**.
- **a,b,...,z**: Represents one of the variables. The  $i$ -th variable is represented by the  $i$ -th lowercase letter in alphabetical order.
- (`<expr>&<expr>`): Represents the logical **and** operation applied to the results of two expressions.
- (`<expr>|<expr>`): Represents the logical **or** operation applied to the results of two expressions.

The logical **and** operation and the logical **or** operation are defined as two boolean functions below that take two boolean values.

$x_1$	$x_2$	$x_1 \& x_2$	$x_1   x_2$
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	1

Determine whether an expression exists that satisfies the conditions. If such an expression exists, ensure that the number of binary operators (& and |) does not exceed  $2^{n-1} + 10$ , and the depth of parentheses nesting does not exceed 100 layers.

It can be proven that if a solution exists, there is always one that meets the constraints of the problem.

## Input

The input consists of multiple test cases. The first line contains an integer  $T$  ( $1 \leq T \leq 2^{16}$ ), the number of test cases. For each test case, there are two lines:

- The first line contains an integer  $n$  ( $1 \leq n \leq 15$ ).
- The second line contains a binary string  $s$  with length  $2^n$ , indicating the truth table of the given function.

To interpret the input binary string, suppose the  $i$ -th variable has a value of  $x_i$ . Then, the corresponding function value,  $f(x_1, x_2, \dots, x_n)$ , is equal to the  $(\sum_{i=1}^n x_i \cdot 2^{i-1} + 1)$ -th bit of the string  $s$ .

It is guaranteed that the sum of  $2^{2^n}$  over all test cases will not exceed  $2^{30}$ .

## Output

For each test case:

- Output **Yes** or **No** on the first line to indicate whether an expression satisfying the conditions exists.
- If an expression exists, output the expression on the second line. The expression must strictly adhere to the format given in the problem description, **without adding or omitting parentheses, and without adding extra spaces**.

### Example

standard input	standard output
7	Yes
2	(a&b)
0001	Yes
2	(a b)
0111	Yes
2	T
1111	Yes
3	((a&(b c)) (b&c))
00010111	No
1	Yes
10	a
2	Yes
0101	(a&(b&(c&(d&e))))
5	
00000000000000000000000000000001	

### Note

Below is the truth table interpretation for the fourth sample.

$x_3$	$x_2$	$x_1$	$f(x_1, x_2, x_3)$
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1