

# Cartesian Trees

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            3 seconds  
Memory limit:         1024 megabytes

You are given a permutation  $A = (A_1, A_2, \dots, A_N)$  of  $(1, 2, \dots, N)$ .

For a pair of integers  $l, r$  ( $1 \leq l \leq r \leq N$ ), we define the **Cartesian Tree**  $C(l, r)$  as follows:

- $C(l, r)$  is a rooted binary tree with  $r - l + 1$  nodes. We denote the root of this tree as  $rt$ .
- Let  $m$  be the unique integer such that  $A_m = \min\{A_l, A_{l+1}, \dots, A_r\}$ .
- If  $l < m$ , then the left subtree of  $rt$  is  $C(l, m - 1)$ . If  $l = m$ , then  $rt$  has no left child.
- If  $m < r$ , then the right subtree of  $rt$  is  $C(m + 1, r)$ . If  $m = r$ , then  $rt$  has no right child.

You are given  $Q$  pairs of integers  $(l_1, r_1), (l_2, r_2), \dots, (l_Q, r_Q)$ . Determine how many different Cartesian Trees are there among  $C(l_1, r_1), C(l_2, r_2), \dots, C(l_Q, r_Q)$ .

Two Cartesian Trees  $X$  and  $Y$  are considered the same if and only if all of the following conditions are satisfied:

- Let the root of  $X$  be  $rt_X$ , and the root of  $Y$  be  $rt_Y$ .
- If  $rt_X$  has a left child, then  $rt_Y$  also has a left child, and the left subtrees of  $rt_X$  and  $rt_Y$  are the same Cartesian Tree.
- If  $rt_X$  has no left child, then  $rt_Y$  also has no left child.
- If  $rt_X$  has a right child, then  $rt_Y$  also has a right child, and the right subtrees of  $rt_X$  and  $rt_Y$  are the same Cartesian Tree.
- If  $rt_X$  has no right child, then  $rt_Y$  also has no right child.

## Input

The input is given in the following format:

```
N
A1 A2 ... AN
Q
l1 r1
l2 r2
⋮
lQ rQ
```

- All input values are integers.
- $1 \leq N \leq 4 \times 10^5$ .
- $A$  is a permutation of  $(1, 2, \dots, N)$ .
- $1 \leq Q \leq 4 \times 10^5$ .
- $1 \leq l_i \leq r_i \leq N$  ( $1 \leq i \leq Q$ ).
- $(l_i, r_i) \neq (l_j, r_j)$  ( $1 \leq i < j \leq Q$ ).

## Output

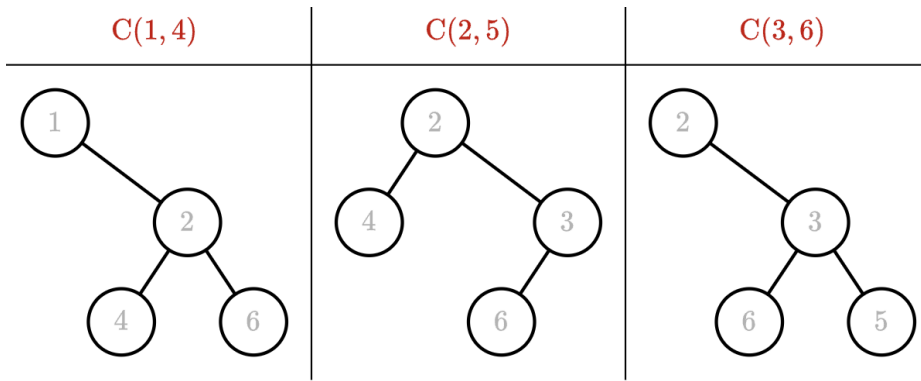
Print the number of different Cartesian Trees among the given pairs  $(l_1, r_1), (l_2, r_2), \dots, (l_Q, r_Q)$ .

## Examples

standard input	standard output
6 1 4 2 6 3 5 3 1 4 2 5 3 6	2
4 1 2 3 4 10 1 1 2 2 3 3 4 4 1 2 2 3 3 4 1 3 2 4 1 4	4
10 3 8 4 7 2 5 9 10 1 6 13 5 8 2 6 7 9 3 8 3 5 2 4 4 6 1 9 3 7 6 9 2 10 4 9 3 9	11

## Note

In the first example,  $C(1, 4), C(2, 5), C(3, 6)$  are the following Cartesian Trees:



$C(1,4)$  and  $C(3,6)$  are the same Cartesian Tree, while  $C(2,5)$  is a different Cartesian Tree from these. Therefore, there are 2 different Cartesian Trees.