

# Problem J

## Menger Sponge

Time limit: 2 seconds

The Menger sponge is a simple 3D fractal. Its level- $L$  approximation can be constructed with the following algorithm:

Start with a single solid  $1 \times 1 \times 1$  cube with opposite corners at  $(0, 0, 0)$  and  $(1, 1, 1)$ .

For each iteration  $i = 1, \dots, L$ :

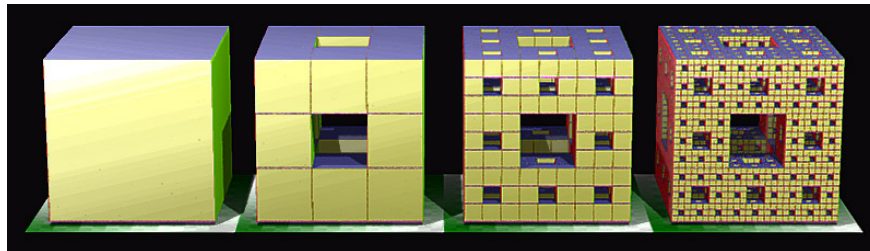
For each cube:

Cut the cube into a regular  $3 \times 3 \times 3$  grid of 27 subcubes.

Delete the seven subcubes that don't touch an edge of the parent cube (see illustration).

The points in the level- $L$  Menger sponge are those that remain after running the above algorithm. Points exactly on the boundary of cubes that remain in the sponge **are** part of the sponge.

The picture below shows the result for  $L = 0$  through  $L = 3$ :



Given a level  $L$  and a point in space given by three rational coordinates, determine if the point is in the level- $L$  Menger sponge.

### Input

The single line of input contains seven integers  $L, x_{\text{num}}, x_{\text{denom}}, y_{\text{num}}, y_{\text{denom}}, z_{\text{num}}, z_{\text{denom}}$ :

$$0 \leq L \leq 10^5$$

$$0 < x_{\text{num}} < x_{\text{denom}} \leq 10^6$$

$$0 < y_{\text{num}} < y_{\text{denom}} \leq 10^6$$

$$0 < z_{\text{num}} < z_{\text{denom}} \leq 10^6$$

where  $L$  is the level of the Menger Sponge and the point in question is  $\left( \frac{x_{\text{num}}}{x_{\text{denom}}}, \frac{y_{\text{num}}}{y_{\text{denom}}}, \frac{z_{\text{num}}}{z_{\text{denom}}} \right)$ .

## Output

Output a single integer, which is 1 if the point is in the level- $L$  Menger Sponge, or 0 if not.

### Sample Input 1

1 0 0 0 1 3 1 3 1 3 3

### Sample Output 1

1

### Sample Input 2

2 49 81 5 6 20 81

### Sample Output 2

1

### Sample Input 3

3 49 81 5 6 20 81

### Sample Output 3

0