

Problem I. From Modular to Rational

Input file: *standard input*
Output file: *standard output*
Time limit: 6 seconds
Memory limit: 256 mebibytes

This is an interactive problem.

Someone picked a positive rational number $x = p/q$ where $1 \leq p, q \leq 10^9$. You may ask at most 10 queries of the kind “? m ”, where $10^9 < m < 10^{12}$ and m is a prime number. For each query, you will get the number y such that $y \equiv pq^{-1} \pmod{m}$. You have to guess the number x .

Interaction Protocol

The first line of input contains a single integer t , the number of test cases ($1 \leq t \leq 10^5$).

For each test case, you may ask at most 10 queries. Each query should be one of two types:

1. “? m ”, where $10^9 < m < 10^{12}$ and m is a prime number,
2. “! p q ”, where $1 \leq p, q \leq 10^9$, meaning that the answer is equal to p/q .

It is guaranteed that the number x in each test case does not change during testing.

Example

standard input	standard output
3	? 1000000007
1	! 1 1
500000004	? 1000000007
	! 2 4
2	? 1000000007
	! 2 1

Note

In the example, you deal with $x = 1/1$, $x = 1/2$, and $x = 2/1$, while always taking $m = 10^9 + 7$.

As you may see, it is not necessary to have $\gcd(p, q) = 1$ as long as $1 \leq p, q \leq 10^9$ and $x = p/q$.