

# Binary Beaver

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            2 seconds  
Memory limit:         512 megabytes

Busy Beaver has an array of  $N$  integers  $a_1, a_2, \dots, a_N$  with  $1 \leq a_i < 2^K$ . As a coder, he loves writing numbers in binary!

Define the *roundness* of an array of positive integers as the total number of trailing 0's in the binary representations of all its elements. For example, the array  $[2, 3, 6, 8, 10]$  is written in binary as  $[10, 11, 110, 1000, 1010]$ , so its roundness is  $1 + 0 + 1 + 3 + 1 = 6$ .

Busy Beaver may choose an integer  $x$  such that  $0 \leq x < 2^K$  and  $x \neq a_i$  for all  $i$ , and then replace every element by  $a_i \oplus x$ , where  $\oplus$  is bitwise XOR. For the current array, find the maximum possible roundness after this operation.

Then,  $Q$  updates will follow. Each query updates  $a_i \leftarrow v$  for some  $1 \leq i \leq N$  and  $1 \leq v < 2^K$ . Note that **updates are persistent**, meaning that each update modifies the array, and subsequent updates should be applied to the current state.

Output the maximum roundness for the initial array, and again after each update.

## Input

The first line contains a single integer  $T$  ( $1 \leq T \leq 10^4$ ) — the number of test cases.

The first line of each test case contains three space-separated integers  $N$ ,  $Q$ , and  $K$  ( $1 \leq N \leq 2 \cdot 10^5$ ,  $0 \leq Q \leq 2 \cdot 10^5$ ,  $1 \leq K \leq 60$ ).

The second line of each test case contains  $N$  space-separated integers  $a_1, \dots, a_N$  ( $1 \leq a_i < 2^K$ ) — the members of the array  $a$ .

The next  $Q$  lines each contain two integers  $i$  and  $v$  ( $1 \leq i \leq N$ ,  $1 \leq v < 2^K$ ), describing an update.

The sum of  $N$  across all test cases does not exceed  $2 \cdot 10^5$ .

The sum of  $Q$  across all test cases does not exceed  $2 \cdot 10^5$ .

## Output

For each test case, output  $Q + 1$  lines.

The first line should contain a single integer — the answer before any updates.

The  $i$ -th of the next  $Q$  lines should contain the answer after the  $i$ -th update.

## Scoring

There are three subtasks for this problem. Let  $\sum N$  denote the sum of  $N$  across all test cases and let  $\sum Q$  denote the sum of  $Q$  across all test cases.

- (20 points):  $\sum N, \sum Q \leq 1000, K \leq 25$ . In addition, it is guaranteed that  $K > 1$ ,  $a_i < 2^{K-1}$  for all  $i$ , and  $v < 2^{K-1}$  in all updates.
- (30 points):  $\sum N, \sum Q \leq 1000, K \leq 25$ .
- (50 points): No additional constraints.

## Example

standard input	standard output
2	5
5 0 3	0
1 1 2 3 4	4
4 4 3	4
1 3 5 7	6
2 4	8
1 4	
3 4	
4 4	

## Note

For the first test case, the optimal value of  $x$  is  $x = 5$ , which gives  $a \oplus 5 = [4, 4, 7, 6, 1]$ . The roundness is 5.

In the second test case, before the first update, since  $x \neq a_i$  for all  $i$ ,  $x$  must be even, implying that all of  $a \oplus x$  are odd, so the answer is 0. After the first update, the array becomes  $a = [1, 4, 5, 7]$ . Here,  $x = 3$  provides the best result with  $a \oplus 3 = [2, 7, 6, 4]$ , with roundness 4.