

# Doremy's Drying Plan (Hard Version)

Input file:            standard input  
Output file:           standard output  
Time limit:            4 seconds  
Memory limit:         1024 megabytes

**The only differences between the two versions of this problem are the constraint on  $k$ , the time limit and the memory limit. You can make hacks only if all versions of the problem are solved.**

Doremy lives in a rainy country consisting of  $n$  cities numbered from 1 to  $n$ .

The weather broadcast predicted the distribution of rain in the next  $m$  days. In the  $i$ -th day, it will rain in the cities in the interval  $[l_i, r_i]$ . A city is called dry if it will never rain in that city in the next  $m$  days.

It turns out that Doremy has a special power. She can choose  $k$  days, and during these days it will not rain. Doremy wants to calculate the maximum number of dry cities after using the special power.

## Input

The input consists of multiple test cases. The first line contains a single integer  $t$  ( $1 \leq t \leq 10^4$ ) — the number of test cases. The description of the test cases follows.

The first line contains three integers  $n$ ,  $m$  and  $k$  ( $1 \leq n \leq 2 \cdot 10^5$ ,  $2 \leq m \leq 2 \cdot 10^5$ ,  $2 \leq k \leq \min(10, m)$ ) — the number of cities, the number of days, and the number of days of rain that Doremy can prevent.

Then,  $m$  lines follow. The  $i$ -th line contains two integers  $l_i, r_i$  ( $1 \leq l_i \leq r_i \leq n$ ) — the rain coverage on day  $i$ .

It is guaranteed that the sum of  $n$  and the sum of  $m$  over all test cases do not exceed  $2 \cdot 10^5$ .

## Output

For each test case, output one integer — the maximum number of dry cities.

## Example

standard input	standard output
6	1
2 3 2	2
1 2	6
1 2	0
1 1	1000
5 3 2	17
1 3	
2 4	
3 5	
10 6 4	
1 5	
6 10	
2 2	
3 7	
5 8	
1 4	
100 6 5	
1 100	
1 100	
1 100	
1 100	
1 100	
1 100	
1000 2 2	
1 1	
1 1	
20 5 3	
9 20	
3 3	
10 11	
11 13	
6 18	

## Note

In the first test case, if Doremy prevents

- rain 1, 2, then city 2 will be dry;
- rain 2, 3, then no city will be dry;
- rain 1, 3, then no city will be dry;

So there is at most 1 dry city.

In the second test case, if Doremy prevents

- rain 1, 2, then city 1, 2 will be dry;
- rain 2, 3, then city 4, 5 will be dry;
- rain 1, 3, then city 1, 5 will be dry.

So there are at most 2 dry cities.

In the third test case, it is optimal to prevent rain 1, 2, 4, 5.

In the fourth test case, there is always a day of rain that wets all the cities and cannot be prevented.