

# Task: MAG

## Magical stones



Day 1. Source file `mag.*`

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Available memory: 32 MB.

Famous stones  $Xi-n-k$  can only be found in Wonderland. Such a stone is simply a granite board with an inscription consisting only of letters  $X$  and  $I$ . Each board contains exactly  $n$  letters. There are not more than  $k$  positions in each board where letters  $X$  and  $I$  are next to each other.

The top and bottom sides of the stones are not fixed, so the stones can be rotated upside-down. For instance two figures below depict exactly the same stone:



Figure 1: Two ways of looking at the same stone. This stone is of type  $Xi-8-3$ , but also  $Xi-8-4$  (and also of any type  $Xi-8-k$  for  $k \geq 3$ ).

No two magic stones in Wonderland are the same, i.e. no two stones contain the same inscription (remember that the upside-down rotation of a stone is allowed).

If it is possible to read the inscription of some stone in two different ways (using the upside-down rotation) then the *canonical representation* of the stone is defined as the lexicographically less\* of these two ways of reading the inscription.

If a stone's inscription is symmetrical, i.e. the upside-down rotation does not change it, then its canonical representation is defined as the unique way of reading this inscription.

**Example:** There are exactly 6 stones of type  $Xi-3-2$ . Their canonical representations written in lexicographical order are: `III`, `IIX`, `IXI`, `IXX`, `XIX` and `XXX`.

Alice is a well-known expert on the  $Xi-n-k$  stones from Wonderland. She would like to create a lexicographical index of the canonical representations of all stones of type  $Xi-n-k$  (for some specific values of  $n$  and  $k$ ). What inscription should be written at position  $i$  of the index, for a given value of  $i$ ?

## Task

Write a programme which:

- reads numbers  $n$ ,  $k$  and  $i$  from the standard input,
- determines the  $i^{\text{th}}$  (in the lexicographical order) canonical representation of a  $Xi-n-k$  stone,
- writes the result to the standard output.

## Input

The first and only line of the standard input contains three integers  $n$ ,  $k$  and  $i$  ( $0 \leq k < n \leq 60$ ,  $0 < i < 10^{18}$ ) separated by single spaces.

\*We say that inscription  $A$  is lexicographically less than  $B$  (assuming that lengths of  $A$  and  $B$  are the same) if  $A$  contains letter  $I$  and  $B$  contains letter  $X$  at the first position where the inscriptions differ.

## Output

The first and only line of the standard output should contain the  $i^{\text{th}}$  (in the lexicographical order) canonical representation of a Xi- $n$ - $k$  stone.

If the number of Xi- $n$ - $k$  stones is less than  $i$  then the first and only line of output should contain expression NO SUCH STONE.

## Example

For the input data:

3 2 5

the correct result is:

XIX

and for the input data:

3 2 7

the correct result is:

NO SUCH STONE