



## Problem L

### Trace of Product of Sparse Square Matrices

Alice was bored in her linear algebra class. She asked her teacher why they were learning any of this. Does linear algebra have *any* real world use whatsoever?

The teacher thought for a few minutes, and eventually came up with this scenario.

Suppose that a genie appears to you and says he will grant you *three wishes* if you can compute the trace of the product of two sparse square matrices  $A$  and  $B$  with integer entries (modulo 1006903069).

First, you will say, “I wish I remembered how matrix notation works!” and the genie will say that  $A$  and  $B$  are  $n \times n$  grids of numbers. In  $A$ , we let  $a_{i,j}$  denote the element in the  $i$ th row from the top and  $j$ th column from the left. The elements of  $B$  are similarly indexed  $b_{i,j}$ . The matrices are sparse, meaning (informally) that they only have a few nonzero entries, relative to their size.

Next, you will say, “That is great, but now I wish I remembered how to do matrix multiplication!” and the genie will remind you that the product  $AB$  is another  $n \times n$  matrix  $C$ , whose elements  $c_{i,j}$  are computed using the following formula:

$$c_{i,j} = \sum_{k=1}^n a_{i,k} b_{k,j}.$$

Finally, you will say, “Okay, but now I really wish I remembered what the trace was!” and the genie will remind you that the trace of a matrix  $C$  is equal to the sum of the elements along its main diagonal, i.e.

$$\text{tr}(C) = \sum_{t=1}^n c_{t,t}.$$

Note that if all the entries of  $A$  and  $B$  are integers, then  $\text{tr}(AB)$  is an integer as well.

The genie points out that he now owes you  $-3$  wishes, since he granted you three wishes which have yet to be paid for. Each wish was valued at PHP 6,264,067.84 at time of granting, with an additional 30% interest for each day it is not paid.

You dummy! You landed yourself in debt with a genie all because you didn’t pay attention in linear algebra class! Your only way out of this mess is to compute  $\text{tr}(AB)$  (mod 1006903069) and collect the original three wishes promised by the genie.

Alice’s teacher apologized and said that he tried really hard, but this was truly the *only* real world application of linear algebra that he could come up with.

But it’s good enough for Alice, who now desperately wants to solve this problem!

#### Input Format

The matrices are sparse, so they will be encoded by specifying the locations and values of their nonzero entries. Formally, the matrix  $A$  is encoded as follows:

- You are given  $k_a$  triples  $(i, j, x)$ , meaning  $a_{i,j} := x$ .
- All given  $(i, j)$  index pairs are distinct, and all other elements of  $A$  not explicitly mentioned in the input are implicitly equal to 0.

The matrix  $B$  is encoded similarly, with its  $k_b$  nonzero entries explicitly enumerated.

The first line of input contains a single integer  $n$ , the size of the matrices.

This is followed by a line containing an integer  $k_a$ . Then,  $k_a$  lines follow, each describing a nonzero entry in  $A$ . Each line contains three space-separated integers  $i$  and  $j$  and  $x$ , meaning  $a_{i,j} := x$ . If some  $(i, j)$  is **not** mentioned in the input, then  $a_{i,j} := 0$ .

This is followed by a line containing an integer  $k_b$ . Then,  $k_b$  lines follow, each describing a nonzero entry in  $B$ . Each line contains three space-separated integers  $i$  and  $j$  and  $x$ , meaning  $b_{i,j} := x$ . If some  $(i, j)$  is **not** mentioned in the input, then  $b_{i,j} := 0$ .

## Output Format

Output a single line, containing the value of  $\text{tr}(AB)$  (mod 1006903069).

## Constraints

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$$3 \leq n \leq 10^5$$

$$1 \leq k_a, k_b \leq 1.5 \times n$$

$$1 \leq i, j \leq n \text{ and } 1 \leq x \leq 10^9 \text{ in each description.}$$

The  $(i, j)$  pairs are distinct across all descriptions for  $A$ , and similarly for  $B$ .

## Sample I/O

Input	Output
3	27
4	
2 1 6	
2 3 6	
3 1 4	
3 2 3	
4	
1 1 2	
1 3 3	
2 3 3	
3 2 1	

## Explanation

You can verify from the definitions that

$$\text{tr} \left( \begin{bmatrix} 0 & 0 & 0 \\ 6 & 0 & 6 \\ 4 & 3 & 0 \end{bmatrix} \begin{bmatrix} 2 & 0 & 3 \\ 0 & 0 & 3 \\ 0 & 1 & 0 \end{bmatrix} \right) = \text{tr} \left( \begin{bmatrix} 0 & 0 & 0 \\ 12 & 6 & 18 \\ 8 & 0 & 21 \end{bmatrix} \right) = 0 + 6 + 21 = 27.$$