

Problem D

Count DFS Graph

You are currently researching a graph traversal algorithm called the Depth First Search (DFS). Starting with an empty list A , the following pseudocode will fill the list A with the visitation order of a DFS algorithm.

```
DFS(v):
    append v to A
    for each u neighbour of v in ascending node number:
        if u is not in A:
            DFS(u)
```

After running $DFS(1)$ from the pseudocode above, you now have a list A containing a permutation of integers from 1 to N . You now wonder how many different simple undirected graphs with N nodes there are that yield the list A that you have. Count the number, modulo 998 244 353.

A graph is simple when there are no self-loops and there is at most one edge connecting each pair of nodes. Two graphs are considered different if there is an edge connecting a pair of nodes in one graph but not the other.

Input

The first line contains an integer N ($2 \leq N \leq 300$). The second line contains a permutation of the first N positive integers, representing the list A . The first element of A is guaranteed to be 1.

Output

A single integer representing the number of different graphs, whose DFS order gives you the list A , modulo 998 244 353.

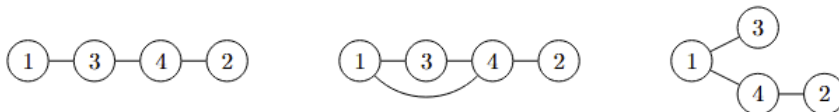
Sample Input 1

```
4
1 3 4 2
```

Sample Output 1

```
3
```

Explanation of Sample 1: The following illustrates all the graphs with the given DFS order.



Sample Input 2

```
10
1 2 3 4 5 6 7 8 9 10
```

Sample Output 2

```
515546413
```



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