

Problem C. Coprime Heaven

Input file: *standard input*
Output file: *standard output*
Time limit: 1 second
Memory limit: 512 mebibytes

The math class is too easy for genius like Nozomi. So she wants to play some single player card game during the class. But since she is a genius, normal single player card game like Solitaire is too easy for her. Thus she creates a hard game called “Coprime Heaven”.

There are n cards in this game, and the i -th card is written with an integer i . At the beginning, she picks m lucky positive integers l_1, l_2, \dots, l_m with $\sum_{i=1}^m l_i = n$. Then she tries to partition the cards into m circles, such that each pair of adjacent cards are coprime.

For example, if $n = 5, m = 2, l_1 = 2, l_2 = 3$, we can partition the cards into two circles $\langle 5, 2 \rangle$ and $\langle 3, 1, 4 \rangle$, since all adjacent pairs $(5, 2), (2, 5), (3, 1), (1, 4), (4, 3)$ are coprime. Note that a circle with only one number will always be valid.

We also want to be as smart as Nozomi, so here are T coprime heaven puzzles for you.

Input

The first line contains an integer T . Each of following T lines contains lucky numbers of one coprime heaven puzzle.

- $1 \leq T \leq 2000$
- $1 \leq m \leq 4$
- $1 \leq l_i \leq 500$
- l_i is sorted in non-decreasing order

Output

For each puzzle, please print a line with “QQ” if there is no valid partition. Otherwise, please print a line with “^_<”. Followed by m lines denote a valid partition. Note that the order of circles should be same as lucky numbers.

Examples

standard input	standard output
4	^_<
1	1
2 3	^_<
4 5 6	2 3
7 8 9 10	5 1 4
	^_<
	1 14 15 8
	6 11 12 5 13
	10 7 4 9 2 3
	QQ