

# Count Triangular Sequences

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            1 second  
Memory limit:         1024 megabytes

A number  $n$  is given. Your task is to count all *triangular sequences* and output the remainder of dividing their count by  $10^9 + 7$ . A sequence is called triangular if it satisfies the following conditions:

- The length of the sequence does not exceed  $n$ .
- Each element is an integer from the interval  $[1, n]$ .
- Some three elements of this sequence can be the lengths of the sides of a non-degenerate triangle\*.

Example triangular sequences for  $n = 100$  are  $(1, 1, 1)$  and  $(16, 1, 11, 25, 100)$ . In the first, the sides of the non-degenerate triangle are  $(1, 1, 1)$ , and in the second, they are  $(16, 11, 25)$ .

The sequence  $(16, 1, 11, 84, 100)$  is not triangular, because no three elements form the sides of a non-degenerate triangle. The sequence  $(5, 5)$  is also not triangular.

## Input

The only line contains an integer  $n$  ( $3 \leq n \leq 200\,000$ ).

## Output

Print a single integer – the remainder of dividing the number of triangular sequences by  $10^9 + 7$  (that is, 1000000007).

## Examples

standard input	standard output
3	15
4	254

## Note

For  $n = 3$  there are 15 triangular sequences:  $(1,1,1)$ ,  $(1,2,2)$ ,  $(1,3,3)$ ,  $(2,1,2)$ ,  $(2,2,1)$ ,  $(2,2,2)$ ,  $(2,2,3)$ ,  $(2,3,2)$ ,  $(2,3,3)$ ,  $(3,1,3)$ ,  $(3,2,2)$ ,  $(3,2,3)$ ,  $(3,3,1)$ ,  $(3,3,2)$ ,  $(3,3,3)$ .

For  $n = 4$  there are 254 triangular sequences:  $(1,1,1)$ ,  $(1,1,1,1)$ ,  $(1,1,1,2)$ ,  $(1,1,1,3)$ ,  $(1,1,1,4)$ ,  $(1,1,2,1)$ ,  $\dots$ ,  $(4,4,2,4)$ ,  $(4,4,3)$ ,  $(4,4,3,1)$ ,  $(4,4,3,2)$ ,  $(4,4,3,3)$ ,  $(4,4,3,4)$ ,  $(4,4,4)$ ,  $(4,4,4,1)$ ,  $(4,4,4,2)$ ,  $(4,4,4,3)$ ,  $(4,4,4,4)$ .

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\*A triangle is non-degenerate if it has a positive area. Equivalently, its vertices are not collinear.