

Circles Are Far from Each Other

Input file: standard input
Output file: standard output
Time limit: 3 seconds
Memory limit: 256 megabytes

You are given n circles and two integer parameters k and ℓ . The i -th circle has radius r_i and $r_i \geq r_j$ holds for every $1 \leq i < j \leq n$. The task is to draw these n circles on a 2D plane so that the following conditions are simultaneously satisfied. Before proceeding to the conditions, let us recall that:

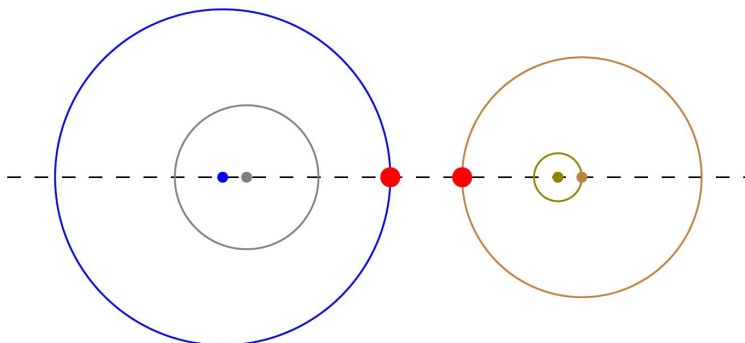
- Each circle is uniquely determined by its center O and radius r .
- A circle of radius r is defined as the set of all points whose distance from its center O is **exactly** r . All distances considered in this task are Euclidean.
- The interior region of a circle is defined as the set of all points whose distance from its center O is **less than** r .
- We say that one circle C encloses another circle C' if all points of C' lie inside the interior region of C .

You need to draw these n circles to satisfy all of the following conditions:

1. The centers of all circles are collinear.
2. The distance between any two centers is at most k .
3. No two circles intersect.
4. If a circle encloses two circles C and C' , then either C encloses C' or C' encloses C .
5. The first ℓ circles **may or may not** be enclosed by other circles, whereas each of the remaining $n - \ell$ circles **must** be enclosed by at least one circle.

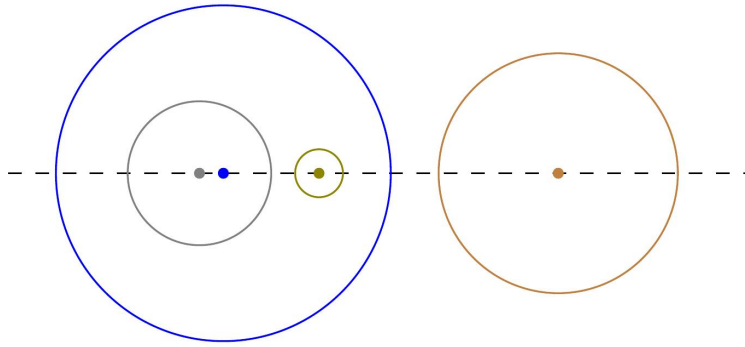
An arrangement that satisfies all the above conditions is called *feasible*. For a feasible arrangement \mathcal{A} , define its *quality* $d(\mathcal{A})$ as the minimum distance between any two points belonging to different circles.

If there exists at least one feasible arrangement for the given case, output the maximum possible quality among all feasible arrangements. If no feasible arrangements exist, output 0.



input 1.

A feasible arrangement for sample



feasible for sample input 1.

An arrangement that is **not**

Input

The first line contains three integers k , n , and ℓ , representing the maximum distance between centers, the number of circles to be drawn, and the number of circles that may or may not be enclosed by other circles, respectively.

The second line contains n integers r_1, r_2, \dots, r_n , where r_i is the radius of the i -th circle.

- $1 \leq k \leq 10^9$
- $2 \leq n \leq 10^5$
- $1 \leq \ell \leq \min\{n, 200\}$
- $1 \leq r_i \leq 10^9$
- $r_i \geq r_j$ for every $1 \leq i < j \leq n$.

Output

If no feasible arrangements exist, output a single integer 0.

Otherwise, output the maximum possible quality $d(\mathcal{A})$ among all feasible arrangements \mathcal{A} in the following format:

- If $d(\mathcal{A})$ is an integer, output it as a single integer.
- If $d(\mathcal{A})$ is not an integer, output it in the rational form a/b such that $1 \leq a, b \leq 10^9$, $\gcd(a, b) = 1$, and $|d(\mathcal{A}) - a/b|$ is minimized. If multiple such forms satisfy the constraints, print any.

Examples

standard input	standard output
15 4 3 7 5 3 1	3
14 6 1 7 5 4 3 2 1	1
14 2 2 5 4	5
22 4 4 4 4 1 1	10/3
13 3 3 6 3 1	4

Note

Explanation of Example 1: A feasible arrangement is illustrated in the first figure, where each circle and its center are shown in a unique color.

In this arrangement, the minimum distance between any two points belonging to different circles is 3, and the two points witnessing this distance are marked as red dots. Hence, the quality of this arrangement is 3, which is the maximum possible among all feasible arrangements for this case. Note that only circle 4 is required to be enclosed within another circle, while the remaining circles may or may not be enclosed.

The second figure shows an arrangement that is **not feasible**. In this case, circle 1 encloses both circle 3 and circle 4, but neither of these two circles encloses the other, thereby violating condition 4.