

## Problem F. Figure Skating

Input file: `figure.in`  
Output file: `figure.out`  
Time limit: 2 seconds  
Memory limit: 512 megabytes

Martian Federation of Figure Skating has adapted the new rules for Mars Figure Skating Championship that will take part in Matrozavodsk on August 31.

The *program* of each competitor consists of a series of *jumps*. There are four jumps that Martians can perform: Axel, Flip, Lutz and Salchow. The program is considered *beautiful* by the judges if it satisfies the following conditions. In all descriptions *arbitrary number of jumps* means 0 or more jumps.

- A *beautiful program* is a *good sequence* of jumps.
- A *good sequence* of jumps starts with an arbitrary number of Axel jumps. After that the sequence can be over, or it can continue with a Flip followed by either *romantic sequence* or *energetic sequence*.
- A *romantic sequence* of jumps starts with arbitrary number of Flip or Lutz jumps (not necessarily all the same) followed by
  - a Lutz jump or a Salchow jump and then an *energetic sequence* or
  - an Axel jump and then a *good sequence*.
- An *energetic sequence* of jumps starts with arbitrary number of Flip jumps followed by a Salchow jump and then a *tragic sequence*.
- A *tragic sequence* of jumps starts with arbitrary number of Flip jumps followed by
  - an Axel jump and then a *romantic sequence*.
  - an Axel jump or a Salchow jump and then an *energetic sequence*.

The rules are so complicated that the judges wonder how many ways are there to create different beautiful programs of exactly  $n$  jumps. Help them find that out. The number can be quite large, so output it modulo 998 244 353.

### Input

The input file contains multiple test cases.

Each test case consists of a single line that contains  $n$  ( $1 \leq n \leq 10^9$ ).

The last test case is followed by a line containing a single zero.

There are at most 1000 test cases.

### Output

For each test case output one integer — the number of jump sequences that make a beautiful program. Output the answer modulo 998 244 353.

### Examples

<code>figure.in</code>	<code>figure.out</code>
1	1
2	2
3	5
4	14
5	42
0	

There are 5 sequences of 3 jumps that make a beautiful program:  $\langle \text{Axel}, \text{Axel}, \text{Axel} \rangle$ ;  $\langle \text{Axel}, \text{Flip}, \text{Axel} \rangle$ ;  $\langle \text{Flip}, \text{Axel}, \text{Axel} \rangle$ ;  $\langle \text{Flip}, \text{Flip}, \text{Axel} \rangle$ ;  $\langle \text{Flip}, \text{Lutz}, \text{Axel} \rangle$ .