

## Problem D. Knapsack and Queries

Input file: *standard input*  
Output file: *standard output*  
Time limit: 10 seconds  
Memory limit: 1024 mebibytes

First, you are given the positive integer  $MOD$ .

You have a knapsack, that is empty at first.

You have to perform  $Q$  queries.

- In each query, you have first to perform either **ADD** or **REMOVE** operation, and then perform **FIND**.
- For **ADD** operation, you are given positive integers  $w$  and  $v$ . You put the cookie with weight  $w$  and value  $v$  to the knapsack.
- For **REMOVE** operation, you take out the cookie with smallest weight from the knapsack and eat it.
- After each **ADD** or **REMOVE** you perform **FIND** operation: given positive integers  $l$  and  $r$ , you answer the follow question: can you choose cookies from that knapsack so that the  $l \leq (X \bmod MOD) \leq r$  ( $X$  is sum of the weight of the selected cookies)?. If you can't, output  $-1$ . Otherwise output the maximum sum of the value of the selected cookies.

### Input

Input is given in the following format:

$MOD$

$Q$

$t'_1 w'_1 v'_1 l'_1 r'_1$

$t'_2 w'_2 v'_2 l'_2 r'_2$

...

$t'_Q w'_Q v'_Q l'_Q r'_Q$

Constraints:

$0 \leq t'_i, w'_i, v'_i, l'_i, r'_i \leq 2^{30} - 1, 2 \leq MOD \leq 500, 1 \leq Q \leq 100\,000$ .

Queries are encrypted as described later. You can get  $t_i, w_i, v_i, l_i, r_i$  by decryption  $t'_i, w'_i, v'_i, l'_i, r'_i$ .

You may assume that  $1 \leq w_i, v_i \leq 10^9, 0 \leq l_i \leq r_i \leq MOD - 1, t_i = 1$  for **ADD+FIND** query,  $t_i = 2$  for **REMOVE+FIND** query (and in this case  $w_i = v_i = 0$ ), that the cookie, which is given by **ADD**, is *heavier* than any cookies which added by the previous **ADD**, and that when executing **REMOVE**, the knapsack isn't empty.

We prepared the decryption code with C++11 (or later), Java, D, C#. Use class `Crypto` for decryption. The code of class `Crypto` and examples of its usage can be uploaded from <http://opentrains.mipt.ru/~ejudge/crypto.zip> for C++11 (or later), Java, D, C#.

Here is the example for C++:

```
#include <cstdint> //uint8_t, uint32_t

class Crypto {
public:
    Crypto() {
```

```
    sm = cnt = 0;
    seed();
}

int decode(int z) {
    z ^= next();
    z ^= (next() << 8);
    z ^= (next() << 16);
    z ^= (next() << 22);
    return z;
}

void query(long long z) {
    const long long B = 425481007;
    const long long MD = 1000000007;
    cnt++;
    sm = ((sm * B % MD + z) % MD + MD) % MD;
    seed();
}

private:
    long long sm;
    int cnt;

    uint8_t data[256];
    int I, J;

    void swap_data(int i, int j) {
        uint8_t tmp = data[i];
        data[i] = data[j];
        data[j] = tmp;
    }

    void seed() {
        uint8_t key[8];
        for (int i = 0; i < 4; i++) {
            key[i] = (sm >> (i * 8));
        }
        for (int i = 0; i < 4; i++) {
            key[i+4] = (cnt >> (i * 8));
        }

        for (int i = 0; i < 256; i++) {
            data[i] = i;
        }
        I = J = 0;

        int j = 0;
        for (int i = 0; i < 256; i++) {
            j = (j + data[i] + key[i%8]) % 256;
            swap_data(i, j);
        }
    }
}
```

```
uint8_t next() {
    I = (I+1) % 256;
    J = (J + data[I]) % 256;
    swap_data(I, J);
    return data[(data[I] + data[J]) % 256];
}
};
```

The decryption process works in the next way:

- First, you make the instance of class `Crypto`.
- For each query first call the `decode` function in order of  $t', w', v', l', r'$ . The return values are  $t, w, v, l, r$ . Then perform the query and call the `query` function with the result of the **FIND**.

The sample C++ code:

```
#include <cstdio>
#include <cstdlib>
#include <cstdint> //uint8_t, uint32_t

class Crypto {
    ...
};

int main() {
    int MOD, Q;
    scanf("%d %d", &MOD, &Q);
    Crypto c;
    for (int i = 0; i < Q; i++) {
        int t, w, v, l, r;
        scanf("%d %d %d %d %d", &t, &w, &v, &l, &r);
        t = c.decode(t);
        w = c.decode(w);
        v = c.decode(v);
        l = c.decode(l);
        r = c.decode(r);
        if (t == 1) {
            (add candy(w, v))
        } else {
            (delete candy)
        }
        long long ans = (answer for query(l, r));
        c.query(ans);
        printf("%lld\n", ans);
    }
}
```

Note that class `Crypto` consume time about 200 to process  $Q = 100\,000$ .

## Output

For each query print the result of **FIND** operation.

## Examples

| standard input                | standard output |
|-------------------------------|-----------------|
| 10                            | 10              |
| 7                             | 0               |
| 281614559 249378726 433981056 | -1              |
| 466775634 683612866           | 21              |
| 727071329 787572584 591471796 | -1              |
| 328464426 757737734           | 11              |
| 279580343 240336097 538846427 | 111             |
| 808491898 224313807           |                 |
| 222498984 42804452 371605808  |                 |
| 667115067 791865961           |                 |
| 68683864 1045549765 515479514 |                 |
| 1067782238 349547144          |                 |
| 907343711 381772625 149003422 |                 |
| 879314974 953881571           |                 |
| 883899098 700164610 414212891 |                 |
| 752949213 972845634           |                 |

| standard input                       | standard output |
|--------------------------------------|-----------------|
| 7                                    | 0               |
| 20                                   | 134             |
| 281614559 249378726 433981094        | 90              |
| 466775639 683612870                  | 158             |
| 59536386 999828879 241246766         | -1              |
| 434670565 174365647                  | 22              |
| 172060134 848462699 857413429        | 238             |
| 182122460 807914643                  | 269             |
| 808426426 600772095 829463884        | 179             |
| 974102196 354283529                  | 189             |
| 370037909 1024921880 664216868       | 121             |
| 194331103 140834169                  | 53              |
| 917331875 242953442 205247688        | 41              |
| 335469789 1055568137                 | 41              |
| 823475244 641321246 617915164        | -1              |
| 160300810 1073617378                 | 58              |
| 892669150 939175632 904628449        | -1              |
| 606339993 1059849410                 | 84              |
| 829170894 436718235 288920513        | -1              |
| 228195002 55212938                   | 149             |
| 772189413 373108543 94133155         |                 |
| 610930061 513937768                  |                 |
| 986619331 175674265 812546186        |                 |
| 865335970 605634588                  |                 |
| 880196843 1071068047 723408215       |                 |
| 587598264 380801783                  |                 |
| 393196081 141080294 584230885        |                 |
| 135343295 661927186                  |                 |
| 5740819 967233824 22597607 888639499 |                 |
| 467454437                            |                 |
| 365679801 515258603 989059385        |                 |
| 962028117 761163096                  |                 |
| 357270919 737051059 569528959        |                 |
| 935653628 70506031                   |                 |
| 869282414 947492121 280522456        |                 |
| 96822010 856514221                   |                 |
| 155948699 826430734 291243254        |                 |
| 381421299 617876780                  |                 |
| 980891674 833928389 1048677341       |                 |
| 522527723 223764850                  |                 |
| 50617939 963598173 281959650         |                 |
| 499436870 47455938                   |                 |

## Note

The result of decoding Sample 1:

```
10
7
1 5 10 5 5
2 0 0 0 9
1 7 10 2 4
1 12 11 9 9
```

2 0 0 1 1  
1 22 10 2 3  
1 32 100 4 4

The result of decoding Sample 2:

7  
20  
1 5 44 0 1  
1 11 90 0 3  
2 0 0 3 4  
1 18 68 1 6  
1 25 32 2 3  
1 31 22 2 3  
1 32 26 1 5  
1 36 31 3 6  
2 0 0 2 5  
1 43 10 3 6  
2 0 0 5 6  
2 0 0 3 4  
2 0 0 2 4  
2 0 0 1 5  
2 0 0 3 5  
1 49 48 0 4  
2 0 0 1 5  
1 50 36 0 6  
1 56 48 3 5  
1 59 17 3 5