

Polynomial Equation

Input file: **standard input**
Output file: **standard output**
Time limit: 1.5 seconds
Memory limit: 1024 megabytes

Busy Beaver has a polynomial equation that he doesn't know how to solve, and he needs your help!

For a bivariate polynomial $P(x, y) = \sum_{i, j \geq 0} a_{i, j} x^i y^j$, define its degree $\deg P = \max_{a_{i, j} \neq 0} (i + j)$. For example, $\deg(x + y + xy) = 2$. Furthermore, we take the degree of the zero polynomial $\deg 0$ to be -1 .

Given a bivariate polynomial $P(x, y)$ with integer coefficients and an integer $d \geq -1$, determine whether there exists a bivariate polynomial $S(x, y)$ and non-constant univariate polynomials Q, R such that

- for $p = 10^9 + 7$, we have

$$(P(x, y) + S(x, y))(Q(x) - Q(y)) = R(x) - R(y)$$

as polynomials in $\mathbb{F}_p[x, y]^*$,

- $\deg S \leq d$.

If a solution exists, output any valid Q, R . **Note that you do not need to output S .**

Input

Each test contains multiple test cases. The first line contains the number of test cases T ($1 \leq T \leq 100$). The description of the test cases follows.

The first line of each test case contains two integers n, d ($1 \leq n \leq 2.5 \cdot 10^3$, $-1 \leq d < n$) — the value of $\deg P$ and the upper bound on $\deg S$, respectively.

The i -th of the next $n + 1$ lines contains $n + 2 - i$ integers $a_{i-1, 0}, \dots, a_{i-1, n+1-i}$ ($0 \leq a_{i, j} < 10^9 + 7$) — the coefficients of P so that $P(x, y) = \sum_{i, j \geq 0, i+j \leq n} a_{i, j} x^i y^j$. It is guaranteed that P has degree n , i.e. at least one of $a_{0, n}, a_{1, n-1}, \dots, a_{n, 0}$ is nonzero.

It is guaranteed that the sum of n across all test cases is no more than $2.5 \cdot 10^3$.

Output

The first line of output for each test case should contain the string “YES” (without quotes) if a solution exists, and “NO” (without quotes) otherwise.

If you claim that a solution exists, continue outputting the solution as follows:

The second line of output for each test case should contain three integers q, r ($1 \leq q, r \leq 5 \cdot 10^3$) — the degrees of the polynomials Q, R respectively.

The third line of output for each test case should contain $q + 1$ integers b_0, \dots, b_q ($0 \leq b_i < 10^9 + 7$, $b_q \neq 0$) — the coefficients of $Q(t) = \sum_{i=0}^q b_i t^i$.

The fourth line of output for each test case should contain $r + 1$ integers c_0, \dots, c_r ($0 \leq c_i < 10^9 + 7$, $c_r \neq 0$) — the coefficients of $R(t) = \sum_{i=0}^r c_i t^i$.

Note that you do not need to output S — the judge will determine if a suitable choice of S exists for your claimed Q, R .

You can output “YES” and “NO” in any case (for example, strings “yES”, “yes” and “Yes” will be recognized as a positive response).

*i.e. when expanded, the two sides of the equation have equal coefficients modulo p .

Scoring

There are five subtasks for this problem.

- (5 points): The sum of n across all test cases is no more than 10, and $d = -1$, i.e. we constrain that S is the zero polynomial.
- (5 points): $d = n - 1$.
- (30 points): $d = -1$, i.e. we constrain that S is the zero polynomial.
- (30 points): The sum of n across all test cases is no more than 500.
- (30 points): No additional constraints.

Example

standard input	standard output
5	YES
2 -1	2 4
40 9 13	20 9 13
9 0	400 360 601 234 169
13	NO
4 2	YES
1000000000 1 1000000001 2 1	2 6
1 1000000000 2 0	1 1 1
999999999 2 1	2 4 7 7 6 3 1
2 0	NO
1	YES
4 2	3 12
1000000000 1 1000000001 2 1	0 2 0 1
1 1000000000 1 0	0 0 0 16 16 24 32 12 24 2 8 0 1
999999999 1 1	
2 0	
1	
4 2	
120 50 61 235 169	
50 81 119 0	
61 119 169	
235 0	
169	
9 5	
17 18 19 20 21 22 2 6 0 1	
16 8 8 4 8 0 2 0 0	
15 8 0 4 0 0 0 0	
14 4 4 2 4 0 1	
13 8 0 4 0 0	
12 0 0 0 0	
2 2 0 1	
6 0 0	
0 0	
1	

Note

In the first test case, the given polynomial is

$$P(x, y) = 13x^2 + 13y^2 + 9x + 9y + 40.$$

We can take $S = 0$, $Q(t) = 13t^2 + 9t + 20$, $R(t) = (13t^2 + 9t + 20)^2$, which gives a valid solution.

In the second test case, it can be shown that no solution exists.