

## Problem K

### $L_\infty$ Jumps

**Input: Standard Input**

**Time Limit: 3 seconds**

Given two points  $(p, q)$  and  $(p', q')$  in the XY-plane, the  $L_\infty$  distance between them is defined as  $\max(|p - p'|, |q - q'|)$ . In this problem, you are given four integers  $n, d, s, t$ . Suppose that you are initially standing at point  $(0, 0)$  and you need to move to point  $(s, t)$ . For this purpose, you perform jumps exactly  $n$  times. In each jump, you must move exactly  $d$  in the  $L_\infty$  distance measure. In addition, the point you reach by a jump must be a lattice point in the XY-plane. That is, when you are standing at point  $(p, q)$ , you can move to a new point  $(p', q')$  by a single jump if  $p'$  and  $q'$  are integers and  $\max(|p - p'|, |q - q'|) = d$  holds.

Note that you cannot stop jumping even if you reach the destination point  $(s, t)$  before you perform the jumps  $n$  times.

To make the problem more interesting, suppose that some cost occurs for each jump. You are given  $2n$  additional integers  $x_1, y_1, x_2, y_2, \dots, x_n, y_n$  such that  $\max(|x_i|, |y_i|) = d$  holds for each  $1 \leq i \leq n$ . The cost of the  $i$ -th (1-indexed) jump is defined as follows: Let  $(p, q)$  be a point at which you are standing before the  $i$ -th jump. Consider a set of lattice points that you can jump to. Note that this set consists of all the lattice points on the edge of a certain square. We assign integer 1 to point  $(p + x_i, q + y_i)$ . Then, we assign integers  $2, 3, \dots, 8d$  to the remaining points in the set in the counter-clockwise order. (Here, assume that the right direction is positive in the  $x$ -axis and the upper direction is positive in the  $y$ -axis.) These integers represent the costs when you perform a jump to these points.

For example, Figure K.1 illustrates the points reachable by your  $i$ -th jump when  $d = 2$  and you are at  $(3, 1)$ . The numbers represent the costs for  $x_i = -1$  and  $y_i = -2$ .

Compute and output the minimum required sum of the costs for the objective.

### Input

The input consists of a single test case.

```
n d s t
x1 y1
x2 y2
⋮
xn yn
```

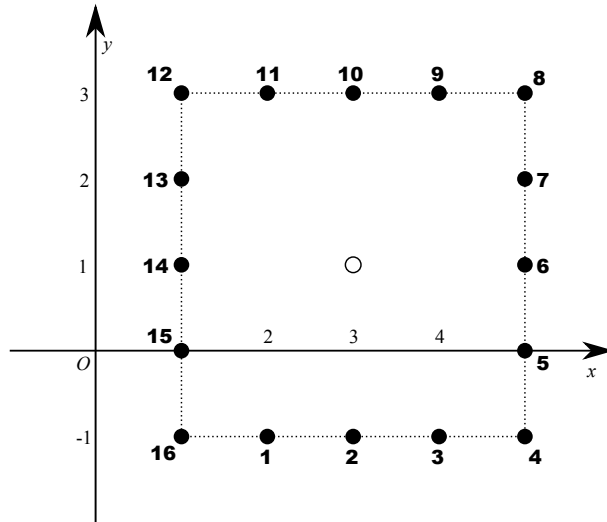


Figure K.1. Reachable points and their costs

The first line contains four integers.  $n$  ( $1 \leq n \leq 40$ ) is the number of jumps to perform.  $d$  ( $1 \leq d \leq 10^{10}$ ) is the  $L_\infty$  distance which you must move by a single jump.  $s$  and  $t$  ( $|s|, |t| \leq nd$ ) are the  $x$  and  $y$  coordinates of the destination point. It is guaranteed that there is at least one way to reach the destination point by performing  $n$  jumps.

Each of the following  $n$  lines contains two integers,  $x_i$  and  $y_i$  with  $\max(|x_i|, |y_i|) = d$ .

## Output

Output the minimum required cost to reach the destination point.

### Sample Input 1

```
3 2 4 0
2 2
-2 -2
-2 2
```

### Sample Output 1

```
15
```

### Sample Input 2

```
4 1 2 -2
1 -1
1 0
1 1
-1 0
```

### Sample Output 2

```
10
```

**Sample Input 3**

```
6 5 0 2
5 2
-5 2
5 0
-3 5
-5 4
5 5
```

**Sample Output 3**

```
24
```

**Sample Input 4**

```
5 91 -218 -351
91 91
91 91
91 91
91 91
91 91
```

**Sample Output 4**

```
1958
```

**Sample Input 5**

```
1 10000000000 -10000000000 -2527532346
8198855077 10000000000
```

**Sample Output 5**

```
30726387424
```