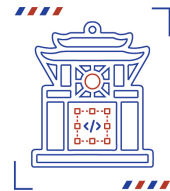




THE 2024 ICPC ASIA PACIFIC CHAMPIONSHIP

VNU UNIVERSITY OF ENGINEERING AND TECHNOLOGY

2ND MARCH 2024



Problem I Symmetric Boundary Time limit: 4 seconds

Symmetrical figures are beautiful—and they are the subject of this task. A region in a 2D plane is *convex* if, for every pair of points p and q in the region, the segment connecting p and q is entirely included in the region. Also, a region in a 2D plane is *point-symmetric* if, when you rotate the region by 180 degrees around a certain point, the rotated region exactly matches the original region.

You are given a convex polygon in a 2D plane with n vertices, numbered from 1 to n in counterclockwise order. Vertex i has coordinates (x_i, y_i) . No three vertices are collinear. Determine whether there exists a convex, point-symmetric region containing all of the n vertices on its boundary. If one or more such regions exist, compute the minimum area among all of them.

Input

The first line of input contains one integer n ($3 \leq n \leq 30$). Each of the next n lines contains two integers. The i -th line contains x_i and y_i ($0 \leq x_i, y_i \leq 1000$).

It is guaranteed that the given polygon is convex, its vertices are given in counterclockwise order, and no three of its vertices are collinear.

Output

If one or more such regions exist, output the minimum area among all of them. The relative error of the output must be within 10^{-9} .

If such a region does not exist, output -1 instead.

Sample Input #1

```
4
0 0
10 0
8 9
4 9
```

Sample Output #1

```
90.0
```

Sample Input #2

```
8
8 10
2 9
0 8
0 2
2 0
8 0
10 2
10 8
```

Sample Output #2

```
-1
```



Sample Input #3

Sample Output #3

6	486567.9669655848
231 77	
359 20	
829 124	
998 461	
941 735	
879 825	

Explanation for the sample input/output

Figure I.1 illustrates the vertices in the sample input as black dots. For sample inputs #1 and #3, the shaded regions represent the regions with the minimum possible area.

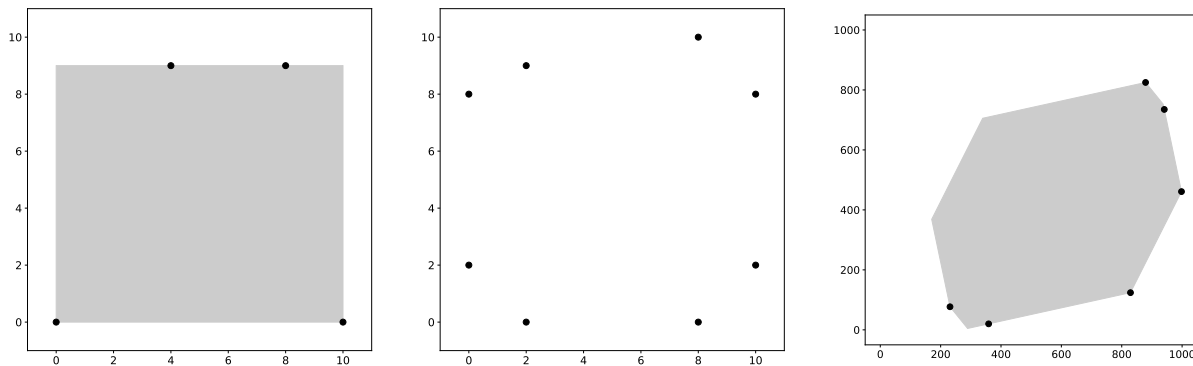


Figure I.1: Illustrations of the sample inputs (from left to right).